



# Scalar similarity and gradient featural representation in Lezgian laryngeal harmony

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## Overview

- Similarity is crucial in evaluating both input-output and surface correspondence in Agreement by Correspondence (Rose and Walker, 2004).
- However, the **representational structure** necessary to compute similarity is often left undefined.
- I encode similarity as a weighted featural lattice in Gradient Harmonic Grammar (Smolensky et al., 2014).
- The gradient representational system correctly predicts patterns of laryngeal consonant co-occurrence in Lezgian, providing a reanalysis of (Ozburn and Kochetov, 2018).

## Lezgian

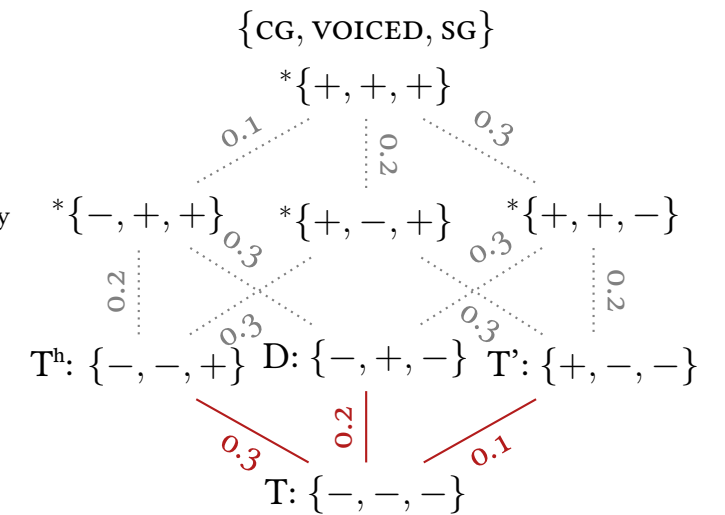
- Co-occurring stops in Lezgian generally agree in LARYNGEAL.
- Yet surprisingly  $T^h \leftrightarrow T$  and  $T \leftrightarrow D$  ( $T'$ =Ejective, T=Voiceless,  $T^h$ =Aspirated, D=Voiced) are also overrepresented in the corpus.
- *Over-represented laryngeal co-occurrences in Lezgian  $O/E > 1$*

Ejective-Ejective	[q'ats'un]	'get dirty'
Voiceless-Voiceless	[qaqa]	'ready'
Voiced-Voiced	[midad]	'grieve'
Aspirated-Aspirated	[tʰipʰ]	'fool'
Aspirated-Voiceless	[kʰutsun]	'to flush'
Voiceless-Voiced	[kudaj]	'hot'

## Proposal

- The challenge is to define similarity as to allow overrepresented but disharmonic exceptions while penalizing the underrepresented structures.
- Perceptual distance/similarity is defined as the summed weights of unshared features:  $distance_w(x, y) = \sum_{f \in \mathcal{F}} w_f \cdot \delta_f(x, y)$  ← categorical similarity
- $\text{CORR}[d \leq k]$  is proposed with respect to the similarity metric: if  $distance \leq k$ , two segments must be in correspondence.
- The weights on features factor into the computation of IDENT-IO and IDENT-CC ( $\mathcal{P} = w \times w_f$ ).

$$\delta_f(x, y) = \begin{cases} 0, & \text{if } x \text{ and } y \text{ share the feature } f \\ 1, & \text{else} \end{cases}$$



Input	Output	$\text{CORR}[d \leq 0.1]$ $w = 20$	ID-CC[LARYNGEAL] $w = 18$	ID-IO[LARYNGEAL] $w = 5$	$\text{CORR}[d \leq 10]$ $w = 0.1$	$\mathcal{H}$
i. /efsɨgun/	a. [efs <sub>x</sub> ig <sub>y</sub> un][ $d = 0.2$ ]				1	-0.1
	b. [efs <sub>x</sub> ik <sub>x</sub> un][ $d = 0$ ]			0.2		-1.0
	c. [efs <sub>x</sub> ik' <sub>x</sub> un][ $d = 0.1$ ]			0.2 + 0.1		-1.5
ii. /qaʃs'un/	a. [q' <sub>x</sub> aʃs' <sub>x</sub> un][ $d = 0$ ]			0.2		-1.0
	b. [q <sub>x</sub> aʃs' <sub>x</sub> un][ $d = 0.1$ ]		0.1			-1.8
	c. [q <sub>x</sub> aʃs <sup>h</sup> <sub>x</sub> un][ $d = 0.3$ ]		0.3	0.3 + 0.1		-7.4
	d. [q <sub>x</sub> aʃs' <sub>y</sub> un][ $d = 0.1$ ]	1			1	-20.1

## Conclusion

- The current study accounts for laryngeal co-occurrence patterns in Lezgian by introducing a gradient featural similarity lattice, over which the intra-featural similarity is evaluated.
- Moreover, the proposed lattice offers a universal structure to link language-specific phonetics to phonological features.

### References:

- Ozburn, Avery and Kochetov, Alexei (2018). Ejective harmony in lezgian. *Phonology*, 35(3):407-440.
- Rose, Sharon and Walker, Rachel (2004). A typology of consonant agreement as correspondence. *Language*, pages 475-531.
- Smolensky, Paul, Goldrick, Matthew, and Mathis, Donald (2014). Optimization and quantization in gradient symbol systems: a framework for integrating the continuous and the discrete in cognition. *Cognitive science*, 38(6):1102-1138.
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